

**Answer the following questions:**

**Q1:(a)** The JFET in the circuit of fig.(1) has  $V_p = -3V$ ,  $I_{DSS} = 9mA$  and  $\lambda = 0$ . Find the values of all resistors so that  $V_G = 5V$ ,  $I_D = 4 mA$  and  $V_D = 11V$ . Design for  $0.05 mA$  in the voltage divider.

**(b)** Find  $V_o/V_s$  for the network shown in fig.(2) if both op amps are considered to be ideal.

**Q2:** The NMOS transistor in the amplifier circuit shown in fig.(3) has  $V_t = 1 V$  and  $K_n = 1mA/V^2$ , and  $V_A = 100V$ .

(a) Determine the  $I_D$ ,  $V_{GS}$ ,  $V_D$ ,  $g_m$  and  $r_o$ .

(b) Determine  $R_{in}$ ,  $R_{out}$ , and the overall voltage gain.

**Q3:** Consider the common gate amplifier shown in fig.(4) with transistor parameter  $g_m = 2mA/V$ . If  $I = 1mA$ ,  $V_{DD} = V_{SS} = 5V$ ,  $R_G = 1 M\Omega$ ,  $R_D = R_L = 3k\Omega$  using T-model determine the small signal voltage gain  $A_v = (v_o / v_i)$ , the input resistance  $R_{in}$ , and the output resistance  $R_{out}$ .

**Q4:** The two op amps in the circuit shown in fig.(5) are ideal. Find  $v_o$ ,  $i_x$  and  $i_o$ .

**Q5:** Find the voltage gain  $v_o/v_i$  and the differential input resistance of the amplifier shown in fig. (6). Assuming  $\beta = 100$ .

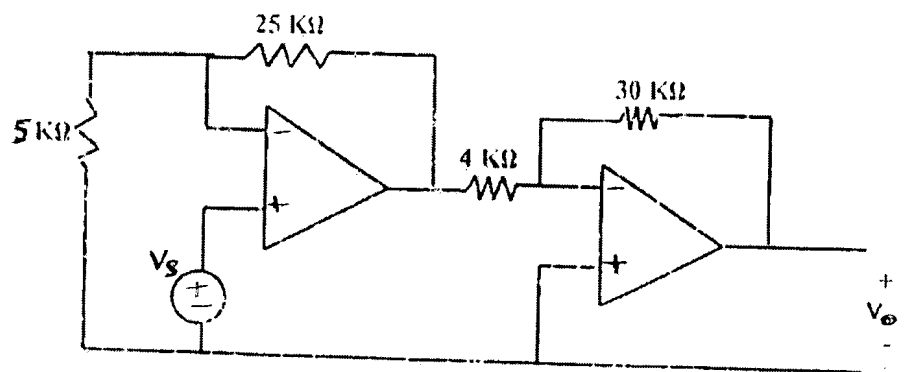
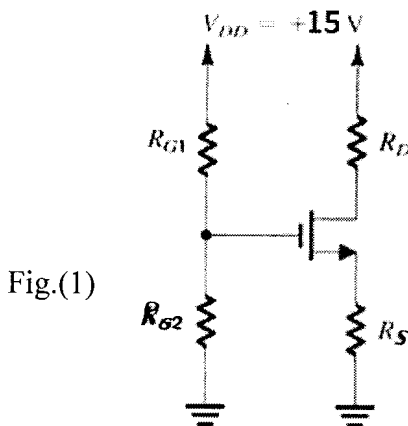


Fig.(2)

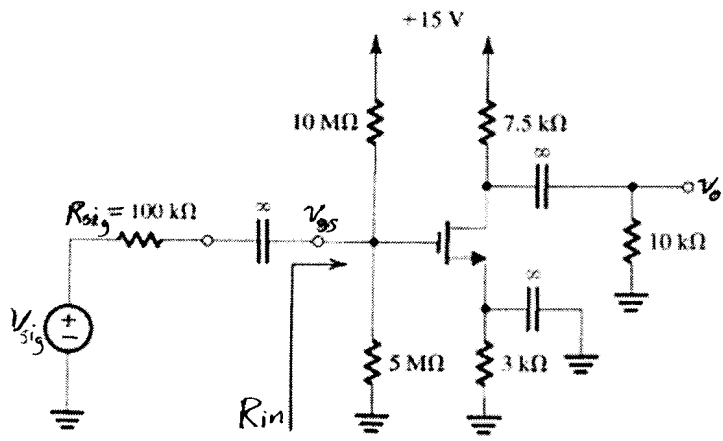


Fig.(3)

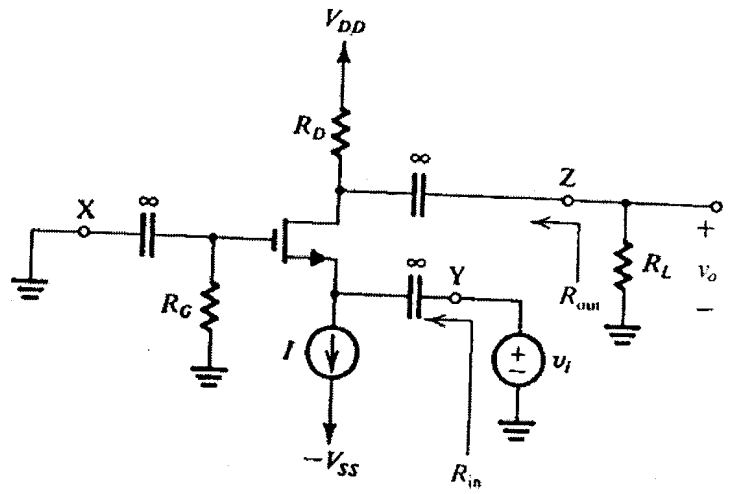


Fig.(4)

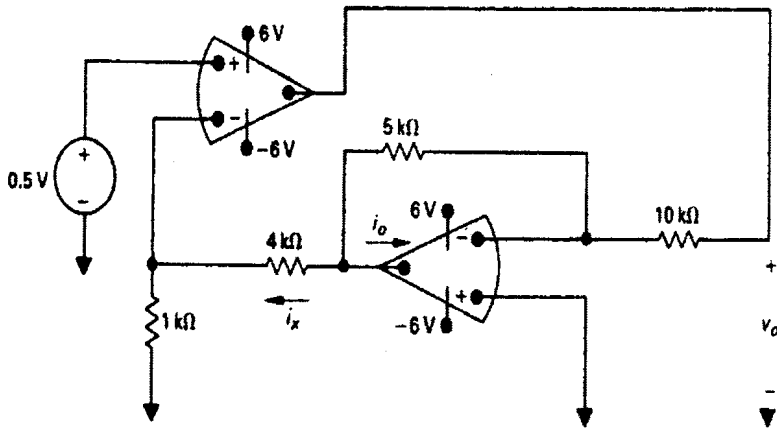


Fig.(5)

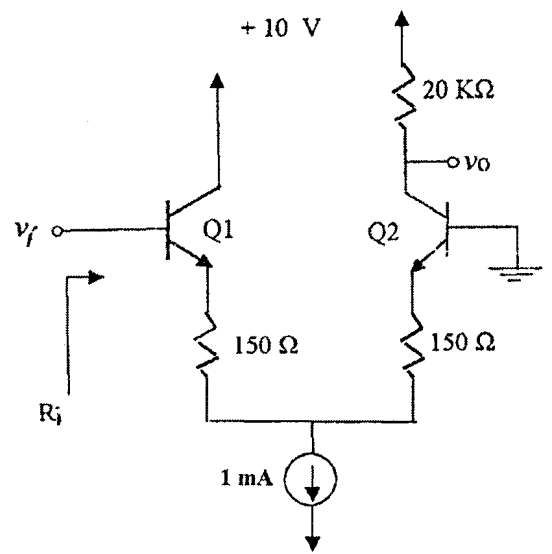
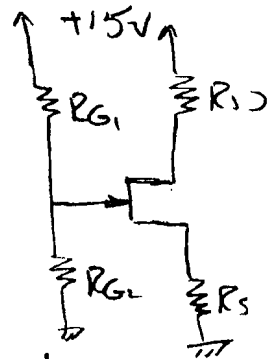


Fig.(6)

***BEST WISHES***

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Q1(a) The JFET in the circuit shown has  $V_p = -3\text{ V}$ ,  $I_{DSS} = 9\text{ mA}$  and  $\lambda = 0$ .  
 Find the values of all resistors so that  $V_G = 5\text{ V}$ ,  $I_D = 4\text{ mA}$  and  $V_D = 11\text{ V}$ ,  
 design for  $0.05\text{ mA}$  in the voltage divider.  
 Solution

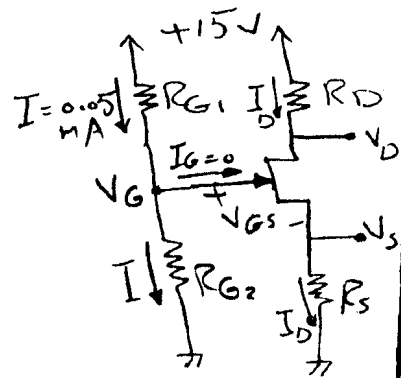


$$\therefore I_G = 0 \text{ \& } V_G = 5\text{ V}$$

$$R_{G1} = \frac{15 - 5}{0.05\text{ mA}} = 200\text{ k}\Omega.$$

$$R_{G2} = \frac{5 - 0}{0.05\text{ mA}} = 100\text{ k}\Omega.$$

$$R_D = \frac{15 - V_D}{I_D} = \frac{15 - 11}{4\text{ mA}} = 1\text{ k}\Omega.$$



$$V_{DS}|_{\text{sat}} = V_{GS} - V_p = V_G - V_S - V_p = 5 - V_S + 3 = 8 - V_S$$

$$V_{DS} = V_D - V_S = 11 - V_S$$

$\therefore V_{DS} > V_{DS}|_{\text{sat}} \therefore$  Tr. in saturation region

$$\therefore I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

$$4\text{ mA} = 9\text{ mA} \left(1 + \frac{V_{GS}}{3}\right)^2 \Rightarrow \frac{4}{9} = \left(1 + \frac{V_{GS}}{3}\right)^2$$

$$\pm \frac{2}{3} = \left(1 + \frac{V_{GS}}{3}\right) \xrightarrow{\times 3} \pm 2 = 3 + V_{GS}$$

$$V_{GS} = \pm 2 - 3 \Rightarrow V_{GS} = -1 \text{ \& } V_{GS} = -5$$

for  $V_{GS} = -5\text{ V} < V_p \Rightarrow$  neglected

then  $V_{GS} = -1\text{ V}$

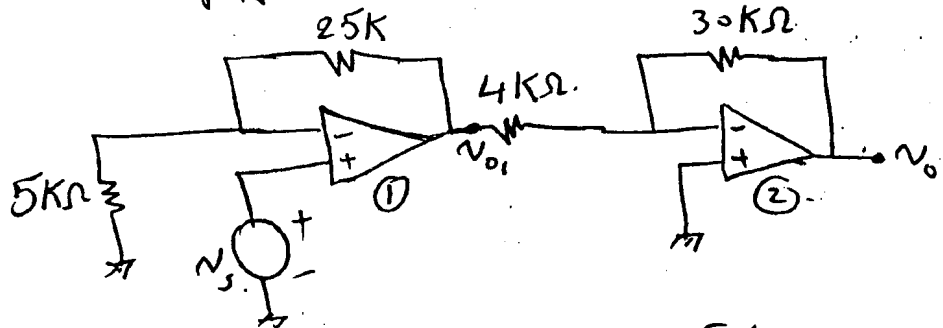
$$\therefore V_{GS} = V_G - V_S \Rightarrow V_S = V_G - V_{GS} = 5 + 1 = 6\text{ V}$$

$$\therefore R_S = \frac{V_S}{I_D} = \frac{6}{4\text{ mA}} = 1.5\text{ k}\Omega.$$

Q. (b).

Find  $\frac{V_o}{V_s}$  for ideal op Amps

Solution



For op Amp ①

∴ non inverting op Amp.

$$\therefore V_{o1} = \left(1 + \frac{R_f}{R_i}\right) V_s$$

$$V_{o1} = \left(1 + \frac{25k}{5k}\right) V_s = (1+5) V_s$$

$$V_{o1} = 6 V_s$$

For op Amp ②

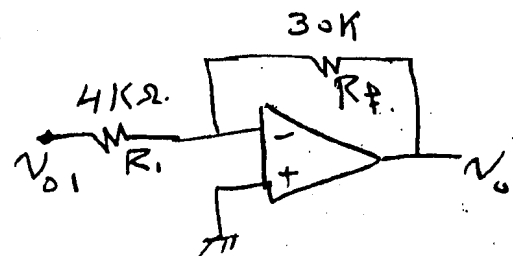
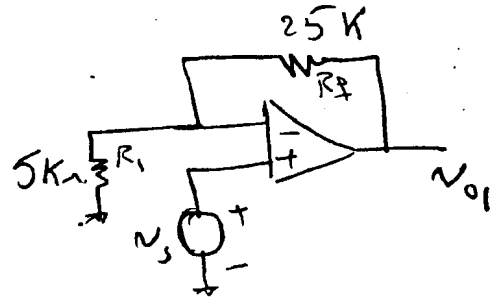
∴ inverting op Amp.

$$V_o = -\frac{R_f}{R_i} V_{o1}$$

$$V_o = -\frac{30k}{4k} V_{o1} = -7.5 V_{o1}$$

$$V_o = -7.5 \times 6 V_s = -45 V_s$$

$$\frac{V_o}{V_s} = -45$$



Q2: (1 points)

The NMOS Transistor in the amplifier circuit shown in Fig. 1 has  $V_t = 1V$ ,  $K_n = 1 \text{ mA/V}^2$ , and  $V_A = 100V$

- (a) Determine  $I_D$ ,  $V_{GS}$ ,  $V_D$ ,  $g_m$  and  $r_o$   
 (b) Determine  $R_{in}$ ,  $R_{out}$ , and the overall voltage gain

Solution

DC Analysis

- All capacitor are o.c
- reduce AC source

$$V_G = \frac{15 \times 5M}{10M + 5M} = 5V$$

$$V_S = 3 \times I_D = 3I_D$$

$$V_{GS} = V_G - V_S = 5 - 3I_D$$

$$\therefore I_D = K_n (V_{GS} - V_t)^2$$

$$= 1(5 - 3I_D - 1)^2$$

$$I_D = (4 - 3I_D)^2$$

$$I_D = (16 - 24I_D + 9I_D^2)$$

$$9I_D^2 - 25I_D + 16 = 0$$

$$(9I_D - 16)(I_D - 1) = 0$$

$$\Rightarrow I_D = \frac{16}{9} = 1.778 \text{ mA} \quad ; \quad I_D = 1 \text{ mA}$$

$$\text{For } I_D = 1.778 \text{ mA} \Rightarrow V_{GS} = 5 - 3 \times 1.778 = -0.33 \text{ V} < V_t \quad \times$$

$$\text{For } I_D = 1 \text{ mA} \Rightarrow V_{GS} = 5 - 3 \times 1 = 2 \text{ V} > V_t \quad \checkmark$$

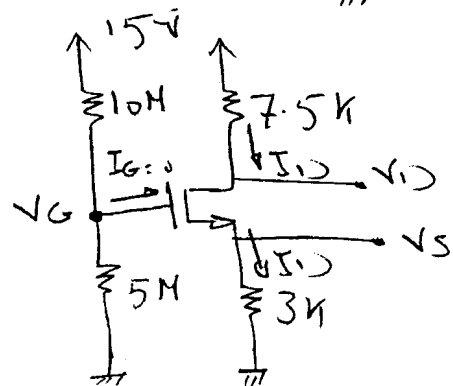
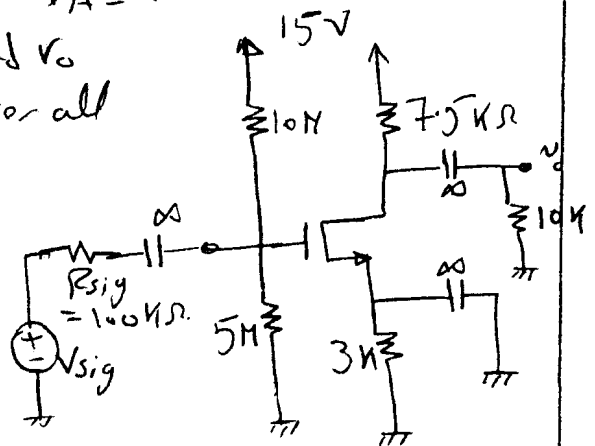
$$\therefore I_D = 1 \text{ mA}$$

$$; \quad V_{GS} = 2 \text{ V}$$

$$V_D = 15 - I_D \times 7.5 = 15 - 1 \times 7.5 = 7.5 \text{ V}$$

$$g_m = 2K_n (V_{GS} - V_t) = 2 \times 1(2 - 1) = 2 \text{ mA/V}$$

$$r_o = \frac{V_A}{I_D} = \frac{100}{1 \text{ mA}} = 100 \text{ k}\Omega$$

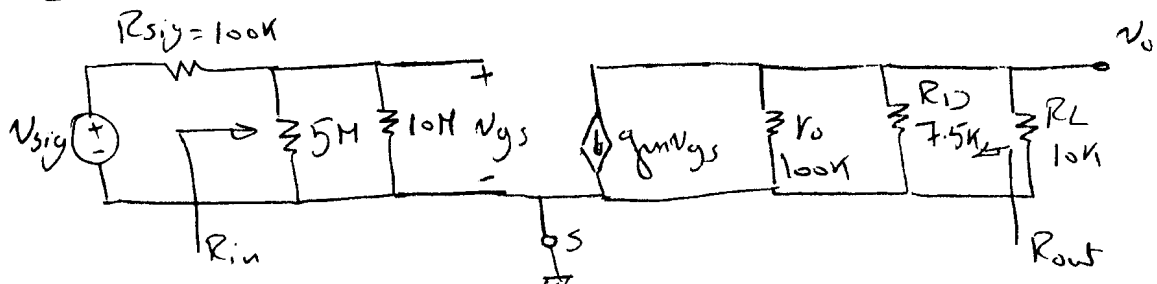
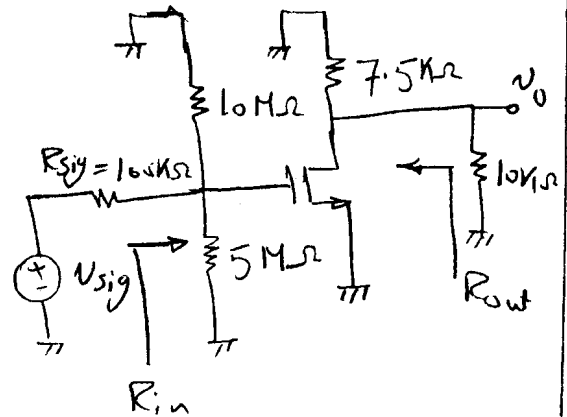


Q2: cont.

## AC Analysis

- All capacitors are s.c
- Reduce DC sources

Using  $\pi$ -Model



$$R_{in} = 5M \parallel 10M = 3.333 M\Omega.$$

$$R_{out}|_{V_{sig}=0} = r_o \parallel R_D = 100k \parallel 7.5k = 6.98 k\Omega.$$

$$v_o = -g_m v_{gs} (r_o \parallel R_D \parallel R_L)$$

$$v_{gs} = v_{sig} \frac{R_{in}}{R_{in} + R_{sig}}$$

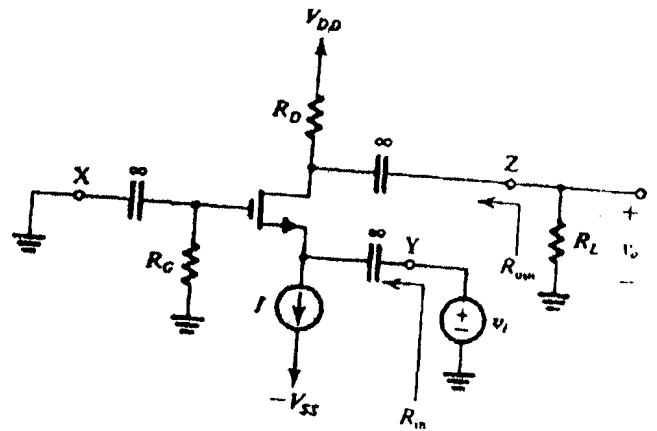
$$v_o = -g_m v_{sig} \frac{R_{in}}{R_{in} + R_{sig}} (r_o \parallel R_D \parallel R_L)$$

$$\therefore A_v = \frac{v_o}{v_{sig}} = -g_m \frac{R_{in}}{R_{in} + R_{sig}} (r_o \parallel R_D \parallel R_L)$$

$$= -2 \times 10^3 \frac{3.333 \times 10^6}{3.333 \times 10^6 + 100k} (100k \parallel 7.5k \parallel 10k)$$

$$= -2 \times 10^3 * 0.971 * 4.11k = -7.98 V/V$$

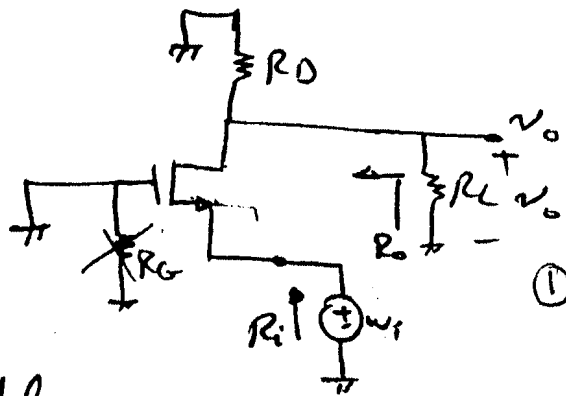
Q3: Consider the common gate amplifier shown in fig. (4) with transistor parameter  $g_m = 2 \text{ mA/V}$ . If  $I = 1 \text{ mA}$ ,  $V_{DD} = V_{SS} = 5 \text{ V}$ ,  $R_G = 1 \text{ M}\Omega$ ,  $R_D = R_L = 3 \text{ k}\Omega$  using T-model determine the small signal voltage gain  $A_v = (v_o/v_i)$ , the input resistance  $R_{in}$ , and the output resistance  $R_{out}$ .



Solution

$$g_m = 2 \text{ mA/V}$$

AC Analysis



Using - T-model

$$R_i = \frac{1}{g_m} = \frac{1}{2 \times 10^{-3}} = 0.5 \text{ k}\Omega \rightarrow \textcircled{2}$$

$$R_o = R_D = 3 \text{ k}\Omega \rightarrow \textcircled{2}$$

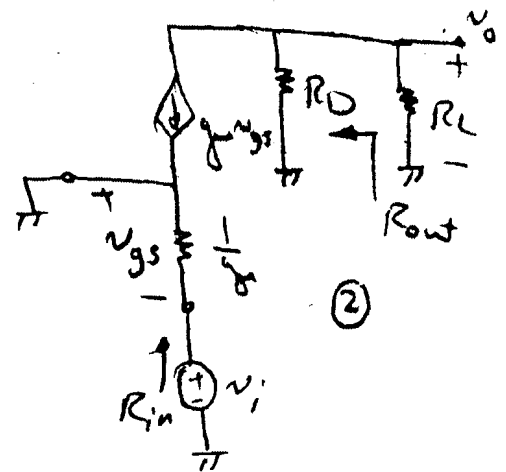
$$v_o = -g_m v_{gs} (R_D \parallel R_L) \rightarrow \textcircled{1}$$

$$v_{gs} = -v_i \rightarrow \textcircled{1}$$

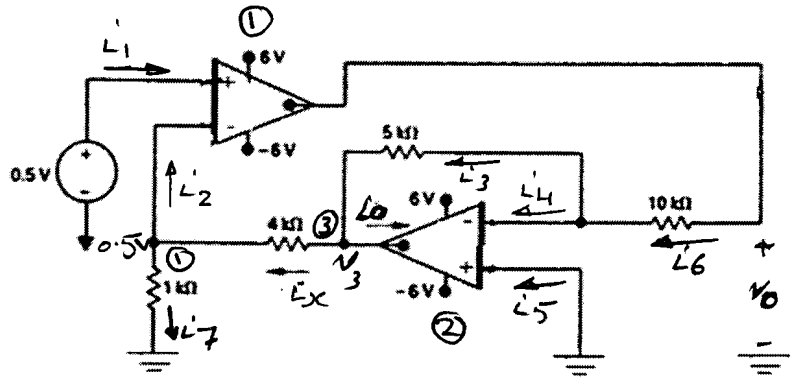
$$v_o = +g_m v_i (R_D \parallel R_L)$$

$$A_v = \frac{v_o}{v_i} = g_m (R_D \parallel R_L) \rightarrow \textcircled{1}$$

$$= 2 \times 10^{-3} (3 \text{ k} \parallel 3 \text{ k}) = 3 \text{ V/V} \rightarrow \textcircled{2}$$



Q4 ) The two op amps in the circuit shown in fig.(5) are ideal. Find  $v_o$ ,  $i_x$  and  $i_o$ .



Solution:

For op Amp ①  $\Rightarrow v_1^+ = v_1^- = 0.5 \text{ V}$

$i_1 = i_2 = 0$

at node ①

$i_2 + i_7 = i_x \quad ; \quad i_2 = 0$

$i_x = i_7 \Rightarrow i_x = \frac{0.5}{1\text{k}} = 0.5 \text{ mA}$

For op AMP ②  $\Rightarrow v_2^+ = v_2^- = 0 \quad ; \quad i_4 = i_5 = 0$

at node ②

$i_6 = i_3 + i_4 \quad ; \quad i_4 = 0$

$i_6 = i_3 \Rightarrow \frac{v_o - v_2^-}{10\text{k}} = \frac{v_2^- - v_3}{5\text{k}} \Rightarrow \frac{v_o}{10\text{k}} = \frac{-v_3}{5\text{k}} \quad *5\text{k}$

$0.5 v_o = -v_3 \Rightarrow v_o = -2 v_3 \quad \text{--- (1)}$

$\therefore v_3 = i_x \times 4\text{k} + 0.5\text{V} = 0.5\text{mA} \times 4\text{k} + 0.5 = 2.5 \text{ V}$

$v_o = -2 \times 2.5 = -5 \text{ V} \quad \Rightarrow \quad v_o = -5 \text{ V}$

at node ③

$i_3 = i_o + i_x \Rightarrow i_o = i_3 - i_x$

$i_o = \frac{-v_3}{5\text{k}} - 0.5\text{mA} = \frac{-2.5}{5\text{k}} - 0.5\text{mA} = -0.5\text{mA} - 0.5\text{mA}$

$i_o = -1 \text{ mA}$



Q5) Find the voltage gain and the input resistance of the amplifier shown in fig.(6) assuming that  $\beta = 100$ .

Solution:

DC Analysis

$$\begin{aligned} \therefore I_{E1} &= I_{E2} = I_E = \frac{I}{2} \\ \therefore I_E &= \frac{1\text{mA}}{2} = 0.5\text{mA} \end{aligned}$$

$$I_C = \alpha I_E = 0.99 I_E$$

$$= 0.99 \times 0.5\text{mA} = 0.494\text{mA} \approx 0.5\text{mA}$$

$$r_e = \frac{V_T}{I_E} = \frac{25\text{mV}}{0.5\text{mA}} = 50\Omega$$

$$g_m = \frac{I_C}{V_T} = \frac{0.5\text{mA}}{25\text{mV}} = 20\text{mA/V}$$

AC Analysis

$$\begin{aligned} \text{Voltage gain } \left| \frac{V_o}{V_i} \right| &= \left| \frac{R_C}{2r_e + 2R_E} \right| \\ &= \frac{20\text{K}}{2(50 + 150)} = 50\text{ V/V} \end{aligned}$$

$$\begin{aligned} R_i &= (1 + \beta)(2r_e + 2R_E) \\ &= 2(1 + \beta)(r_e + R_E) \end{aligned}$$

$$= 2(1 + 100)(50 + 150) = 40.4\text{ k}\Omega.$$

