



Answer the following questions:

- Q1: (a)** Assuming that the diodes in the circuit of Fig.(1) are ideal, find the values of the labeled voltage, V , and current, I .
(b) In fig.(2), the first transistor Q_1 has a current gain of 100 and the second transistor Q_2 has a current gain of 50, what is the base current in the first transistor?

- Q2: (a)** Determine and sketch the output waveform for the network of Fig. (3).
(b) What is the output voltage in Fig.(4). Let β of the two transistors are very high.

- Q3:** The 6.8V zener diode in the circuit of Fig.(5) is specified to have $V_z = 6.8V$ at $I_z = 5mA$, $r_z = 20\Omega$, and $I_{zk} = 0.2 mA$. The supply voltage V^+ is nominally 10V but can vary by $\pm 1 V$.
(a) Find V_o with no load and with V^+ at its nominal value.
(b) Find the change in V_o resulting from the $\pm 1 V$ change in V^+ .
(c) Find the change in V_o when $R_L = 2 k\Omega$.
(d) What is the minimum value of R_L for which the diode still operates in the breakdown region?

- Q4:** In the circuit of Fig.(6), v_{sig} is a small sine-wave signal with zero average value. For $V_{CC} = 15V$, $R_1 = R_2 = 100K\Omega$, $R_E = 200 \Omega$, $R_C = R_L = 20 K\Omega$, and $\beta = 100$. Find using hybrid- π model the values of R_{in} , R_o , the voltage gain (v_o/v_{sig}), and the current gain (i_o/i_i).

- Q5:** For the universal BJT amplifier configuration as shown in fig. (7), let $R_B = 100 K\Omega$, $R_C = R_E = 10 K\Omega$, $V_{CC} = V_{EE} = 10V$, $\beta = 100$, and $I_C = 0.838 mA$. If the amplifier is connected in the common base configuration draw the complete circuit of the amplifier and then find using T-model the values of R_i , R_o , A_v , and A_i for $R_S = R_L = 10 K\Omega$.

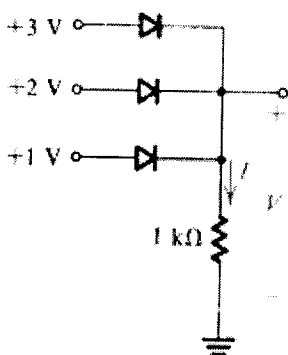


Fig.(1)

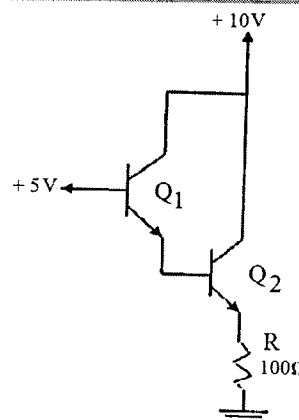


Fig.(2)

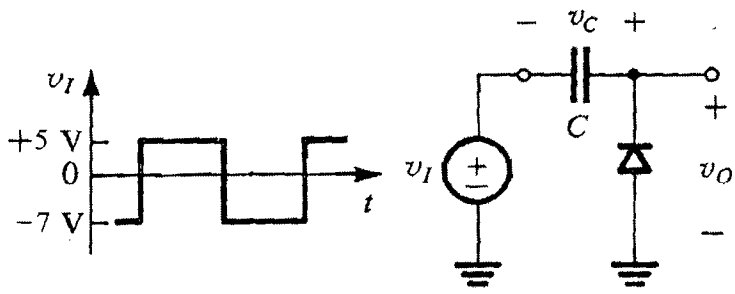


Fig.(3)

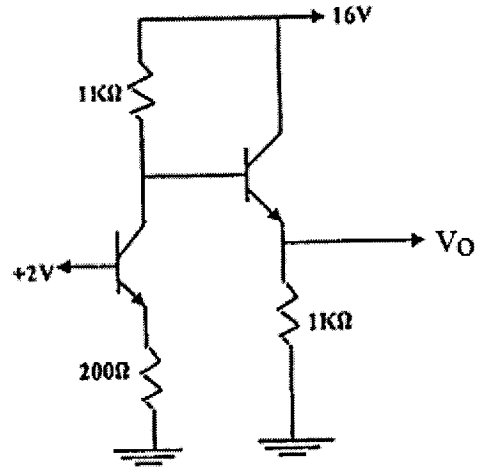


Fig.(4)

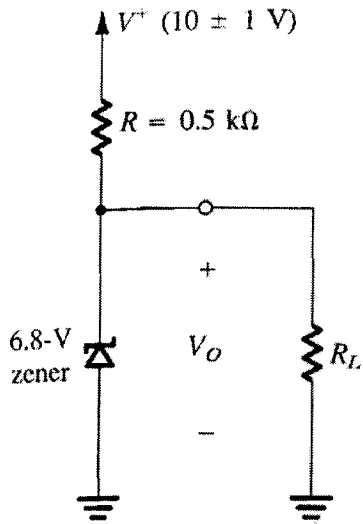


Fig.(5)

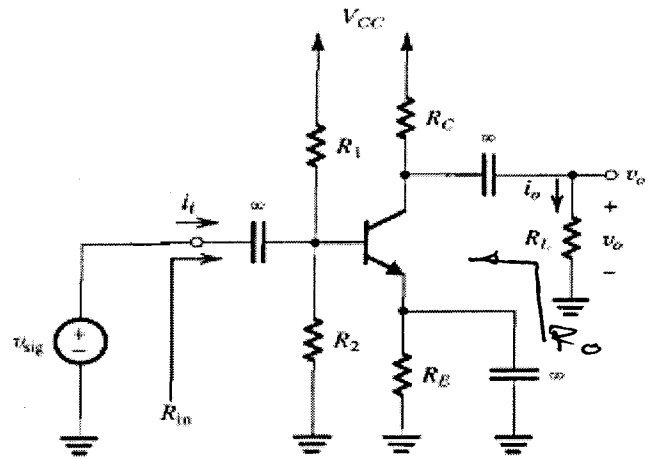


Fig.(6)

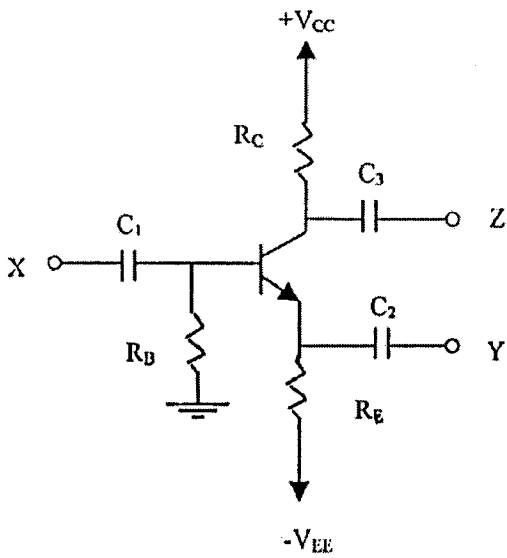


Fig.(7)

BEST WISHES

Hossam Labib

Q1: (b)

The first transistor has a current gain of 100 and the second transistor has a current gain of 50, what is the base current in the first transistor?

Solution

Let 2-transistor in Active region.
Loop (2)

$$-5 + V_{BE1} + V_{BE2} + I_{E2} R_{E2} = 0$$

$$I_{E2} = \frac{5 - 0.7 - 0.7}{100} = 36 \mu A$$

$$I_{B2} = \frac{I_{E2}}{1 + \beta_2} = \frac{36 \mu A}{51} = 7.058 \mu A$$

$$\therefore I_{E1} = I_{B2} = 7.058 \mu A$$

$$\therefore I_{B1} = \frac{I_{E1}}{1 + \beta_1} = \frac{7.058 \mu A}{101} = 7 \mu A$$

$$V_{B1} = 5 V$$

$$V_{E1} = V_{B2} = 5 - V_{BE1} = 4.3 V$$

$$V_{C1} = V_{C2} = 10 V$$

$$V_{E2} = I_{E2} R_{E2} = 36 \mu A \times 100 = 3.6$$

$$V_{B1} > V_{E1} \Rightarrow BE_1 \text{ Forward}$$

$$V_{C1} > V_{B1} \Rightarrow BC_1 \text{ reverse}$$

$\therefore Q_1$ in Active region

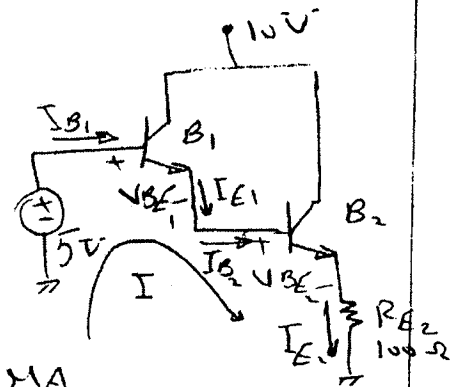
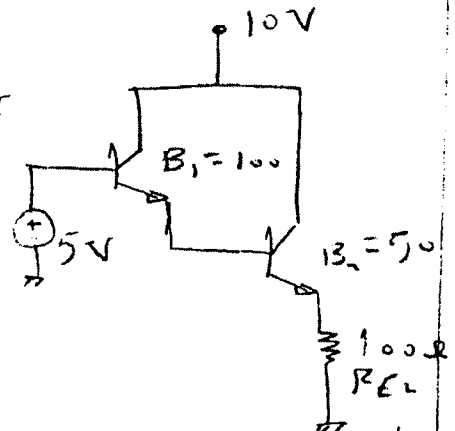
$$V_{B2} > V_{E2} \Rightarrow BE_2 \text{ Forward}$$

$$V_{C2} > V_{B2} \Rightarrow BC_2 \text{ reverse}$$

$\therefore Q_2$ in Active region

\therefore ASSUMPTION TRUE

$$\therefore I_{B1} = 7 \mu A$$



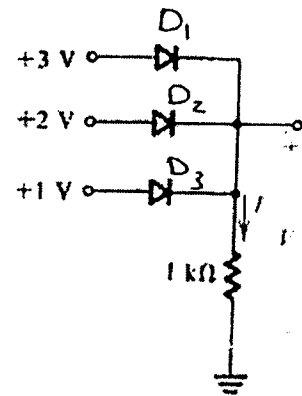
Q₁(a) Find the values of I and V in the circuits shown in Fig. (1).

For Fig. (a)

for D₁ on $\Rightarrow V=3V$ D₂ and D₃ are off

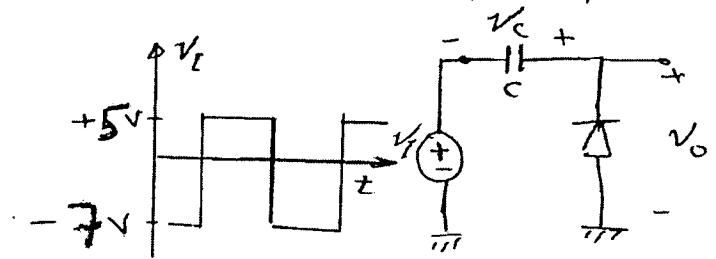
$$\therefore V = 3V$$

$$I = \frac{V}{R} = \frac{3}{1k\Omega} = 3mA$$



Q2: (a) points

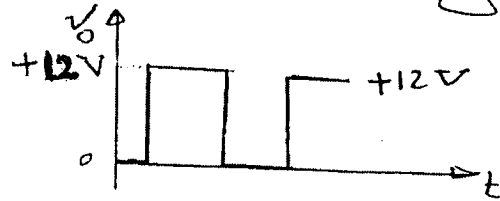
Q2: (a) Determine and sketch the output waveform for the network shown



$$V_c = 7 \text{ V}$$

$$v_o = v_i + V_c \\ = v_i + 7$$

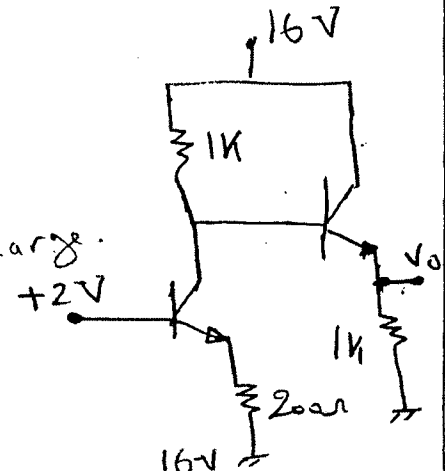
i.e. $v_o = v_i + \text{shifted by } -ve \text{ half cycle}$



Q2(b)

What is the o/p voltage.

- Let β of the 2-transistors is very large.



Solution

$\therefore \beta$ is very high

$$\therefore I_{B1} \approx I_{B2} \approx 0$$

Loop (I) Let Q_1 and Q_2 in Active region

$$-2 + V_{BE1} + I_{E1} R_{E1} = 0$$

$$I_{E1} = \frac{2 - 0.7}{200} = 6.5 \text{ mA}$$

$$\therefore I_{C1} = I_{E1}$$

$$\therefore \text{at node } \textcircled{1} \Rightarrow I_1 = I_{C1} + I_{B2} \quad ; \quad I_{B2} = 0$$

$$\therefore I_1 = I_{C1} = 6.5 \text{ mA}$$

$$V_{C1} = 16 - I_1 \times 1k = 16 - 6.5 \times 1 = 9.5 \text{ V} = V_{B2}$$

$$V_{E1} = I_{E1} R_{E1} = 6.5 \times 0.2 = 1.3 \text{ V}$$

Loop (II)

$$-V_{C1} + V_{BE2} + I_{E2} R_{E2} = 0$$

$$I_{E2} = \frac{9.5 - 0.7}{1k} = 8.8 \text{ mA}$$

$$\therefore V_o = I_{E2} R_{E2} = 8.8 \times 1 = 8.8 \text{ V} = V_{E2}$$

$$V_{C2} = 16 \text{ V}$$

for Q_1 $\therefore V_{B1} > V_{E1} \Rightarrow BEJ \rightarrow$ Forward

$V_{B1} < V_{C1} \Rightarrow BCJ \rightarrow$ Reverse

$\therefore Q_1$ in Active region

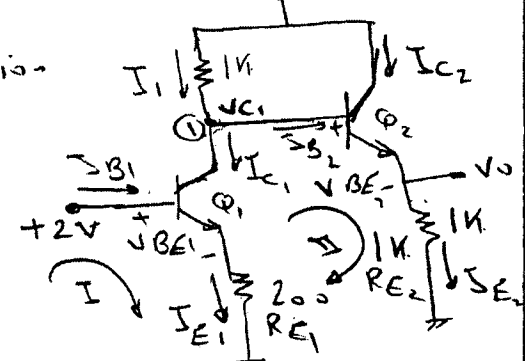
for Q_2 $\therefore V_{B2} > V_{E2} \Rightarrow BEJ \rightarrow$ Forward.

$V_{B2} < V_{C2} \Rightarrow BCJ \rightarrow$ Reverse

$\therefore Q_2$ in Active region

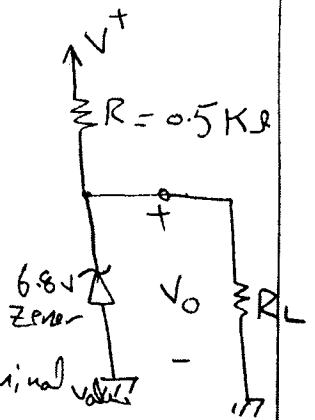
\therefore Assumption is True.

$$\therefore V_o = V_{E2} = 8.8 \text{ V}$$



Q3: - (3 points)

The 6.8 V Zener diode in the circuit shown is specified to have $V_Z = 6.8 \text{ V}$ at $I_Z = 5 \text{ mA}$, $r_Z = 20 \Omega$, and $I_{ZK} = 0.1 \text{ mA}$. The supply voltage V^+ is nominally 10 V but can vary by $\pm 1 \text{ V}$.



(a) Find V_0 with no load and with V^+ at its nominal value.

$$\therefore V_Z = V_{Z0} + r_Z I_Z$$

$$6.8 = V_{Z0} + 20 \times 5 \times 10^{-3}$$

$$\therefore V_{Z0} = 6.8 - 0.1 = 6.7 \text{ V}$$

with no load i.e. $R_L = \infty$

$$I = I_Z = \frac{V^+ - V_{Z0}}{R + r_Z}$$

$$= \frac{10 - 6.7}{0.5 \text{ k} + 20} = 6.35 \text{ mA}$$

$$\therefore V_0 = V_{Z0} + I_Z r_Z$$

$$= 6.7 + 6.35 \times 20 = 6.83 \text{ V}$$

(b) Find the change in V_0 resulting from the $\pm 1 \text{ V}$ change in V^+ . The change in V_0 can be found from

$$\Delta V_0 = \Delta V^+ \frac{r_Z}{R + r_Z}$$

$$= \pm 1 \times \frac{20}{0.5 \text{ k} + 20} = \pm 38.5 \text{ mV}$$

(c) Find the change in V_0 when $R_L = 2 \text{ k}\Omega$

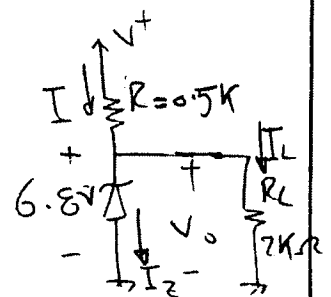
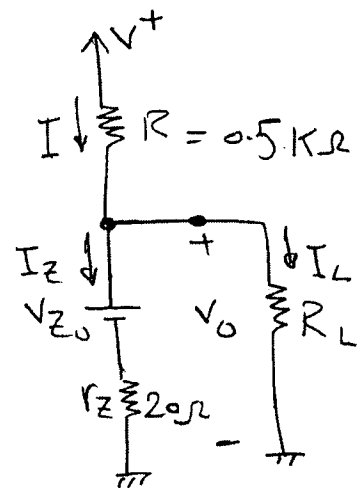
If $R_L = 2 \text{ k}\Omega$ is connected

$$\therefore I_L \approx \frac{V_Z}{R_L} \Rightarrow \frac{6.8}{2 \text{ k}} = 3.4 \text{ mA}$$

$$I = \frac{10 - 6.8}{0.5 \text{ k}} = 6.4 \text{ mA}$$

$$\therefore I = I_Z + I_L \Rightarrow I_Z \Big|_{\text{Loaded}} = I - I_L =$$

$$I_Z \Big|_{\text{Loaded}} = 6.4 \text{ mA} - 3.4 \text{ mA} = 3 \text{ mA}$$



Q3: (cont.)

change in Zener current $\Delta I_Z = I_Z|_{\text{Load}} - I_Z|_{\text{No-Load}}$
 $\Delta I_Z = 3 - 6.35 = -3.4 \text{ mA}$

\therefore change in $V_0 \Rightarrow \Delta V_0 = \Delta I_Z V_Z$

$$\Delta V_0 = -3.4 \text{ mA} \times 20 = -68 \text{ mV}$$

(d) what is the min. value of R_L for which the diode still operates in the breakdown region?

For the Zener at edge of the breakdown region then $I_Z = I_{ZK} = 0.2 \text{ mA}$ and $V_{Z0} \approx V_{ZK} \approx 6.7 \text{ V}$

\therefore At this point the lowest current supplied through R

$$I = \frac{V^+ - V_{ZK}}{R}$$

$$= \frac{9 - 6.7}{0.5 \text{ k}} = 4.6 \text{ mA}$$

$$\therefore I_L = I - I_Z = 4.6 - 0.2 = 4.4 \text{ mA}$$

$$R_L|_{\text{min}} = \frac{V_0}{I_L} \approx \frac{V_Z}{I_L}$$

$$= \frac{6.7}{4.4 \text{ mA}} = 1.5 \text{ k}\Omega$$

Q4: (Points)

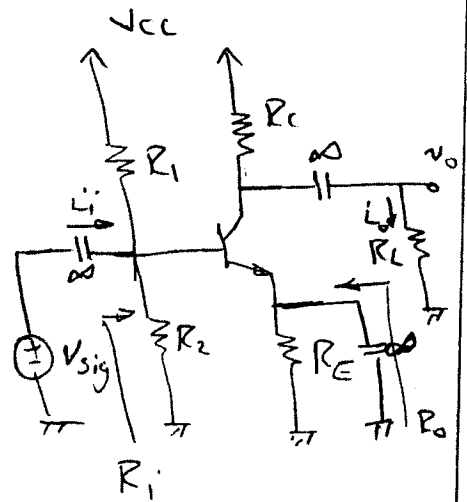
In the circuit of Fig. (1), V_{sig} is a small sine-wave signal with zero average value. For $V_{CC} = 15\text{ V}$,

$$R_1 = R_2 = 100\text{ k}\Omega, R_E = 200\Omega$$

$$R_C = R_L = 20\text{ k}\Omega, \text{ and } \beta = 100. \text{ Find}$$

Using hybrid- π model the values of R_{in} , R_o , the voltage gain $(\frac{V_o}{V_{sig}})$, and the current gain $(\frac{I_o}{I_i})$.

Solution



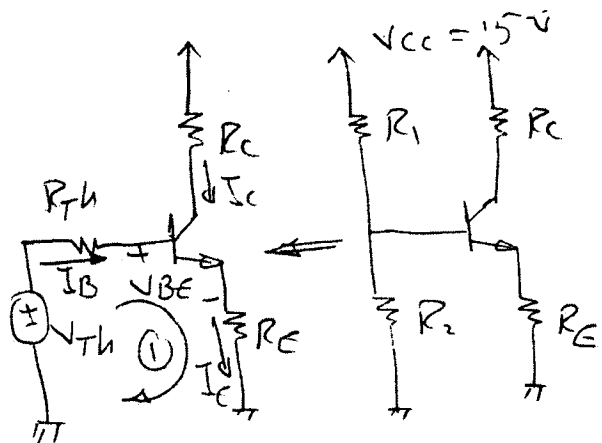
DC Analysis

- All cap. o.c
- reduce AC sources

$$R_{TH} = R_1 \parallel R_2$$

$$= 100\text{ k} \parallel 100\text{ k} = 50\text{ k}\Omega$$

$$V_{TH} = \frac{V_{CC} R_2}{R_1 + R_2} = \frac{15 \times 100\text{ k}}{100\text{ k} + 100\text{ k}} = 7.5\text{ V}$$



Loop (1)

$$-V_{TH} + I_B R_{TH} + V_{BE} + I_E R_E = 0$$

$$\therefore I_E = (1 + \beta) I_B$$

$$-V_{TH} + I_B R_{TH} + V_{BE} + (1 + \beta) I_B R_E = 0$$

$$I_B (R_{TH} + (1 + \beta) R_E) = V_{TH} - V_{BE}$$

$$I_B = \frac{V_{TH} - V_{BE}}{R_{TH} + (1 + \beta) R_E} = \frac{7.5 - 0.7}{50\text{ k} + 101 \times 200} = 96.87\text{ }\mu\text{A}$$

$$I_C = \beta I_B = 100 \times 96.87\text{ }\mu\text{A} = 9.687\text{ mA}$$

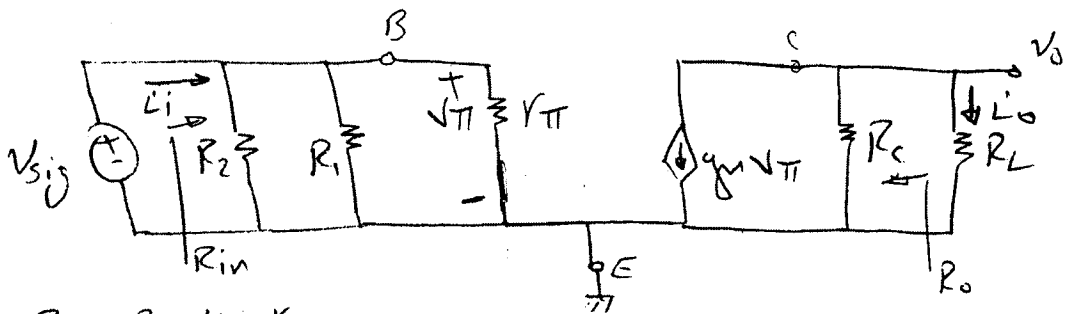
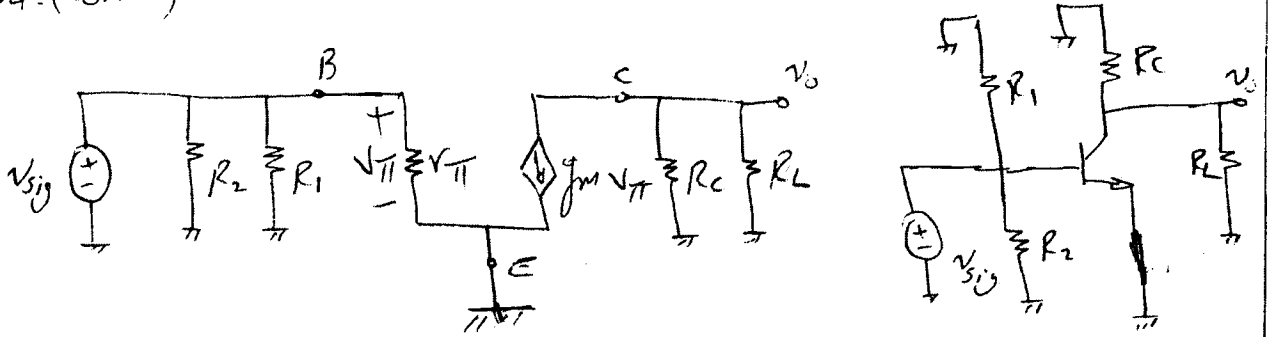
$$g_m = \frac{I_C}{V_T} = \frac{9.687\text{ mA}}{25\text{ mV}} = 0.388\text{ A/V}$$

$$r_{\pi} = \frac{\beta}{g_m} = \frac{100}{0.388} = 258\text{ }\Omega$$

AC Analysis

- All cap. sc & reduce DC sources

Q4: (Cont.)



$$R_{in} = R_1 \parallel R_2 \parallel r_{\pi}$$

$$= 100k \parallel 100k \parallel 258$$

$$= 50k \parallel 258 = 256.68 \Omega$$

$$R_o \Big|_{v_{sig}=0} = R_c = 20k\Omega$$

$$v_o = -g_m v_{\pi} (R_c \parallel R_L)$$

$$v_{\pi} = v_{sig}$$

$$v_o = -g_m v_{sig} (R_c \parallel R_L)$$

$$A_v = \frac{v_o}{v_{sig}} = -g_m (R_c \parallel R_L) = -g_m (R_c \parallel R_L)$$

$$= -0.388 * (20k \parallel 20k) = -3880 \text{ V/V}$$

$$i_o = -g_m v_{\pi} \frac{R_c}{R_c + R_L}$$

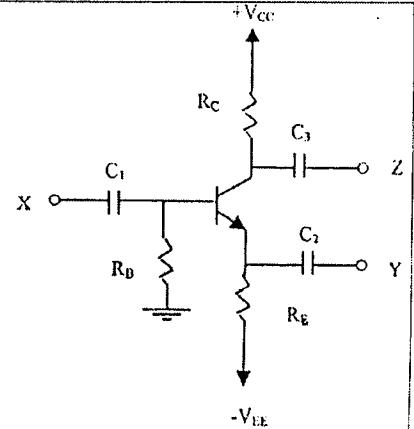
$$\therefore v_{sig} = i_i R_{in} \quad ; \quad v_{\pi} = v_{sig}$$

$$\therefore v_{\pi} = i_i R_{in}$$

$$i_o = -g_m (i_i R_{in}) \left(\frac{R_c}{R_c + R_L} \right)$$

$$A_i = \frac{i_o}{i_i} = -g_m R_{in} \left(\frac{R_c}{R_c + R_L} \right) = -0.388 * 256.68 * \frac{20k}{40k} = -49.8 \text{ A/A}$$

Q5: For the universal BJT amplifier configuration as shown in fig. (7), let $R_B = 100\text{ K}\Omega$, $R_C = R_E = 10\text{ K}\Omega$, $V_{CC} = V_{EE} = 10\text{V}$, $\beta = 100$, and $I_C = 0.838\text{ mA}$. If the amplifier is connected in the common base configuration draw the complete circuit of the amplifier and then find using T-model the values of R_i , R_o , A_v , and A_i for $R_S = R_L = 10\text{ K}\Omega$.



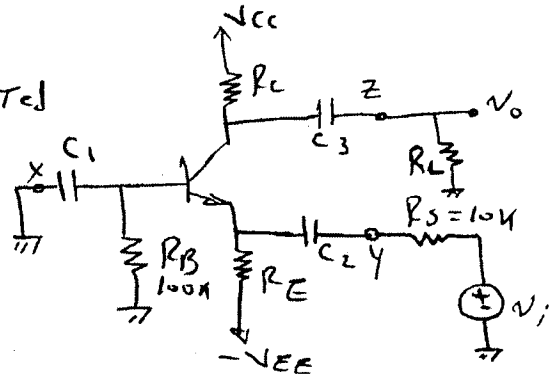
Solution

For $I_C = 0.838\text{ mA}$ then

$$g_m = \frac{I_C}{V_T} = \frac{0.838\text{ mA}}{25\text{ mV}} = 33.52\text{ mA/V}$$

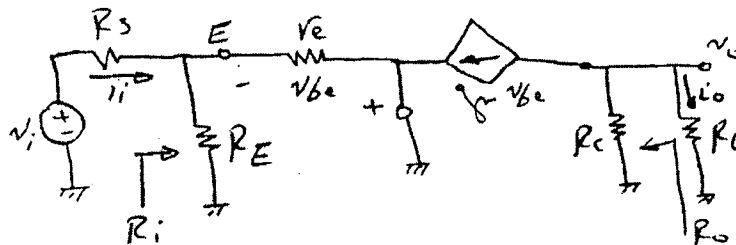
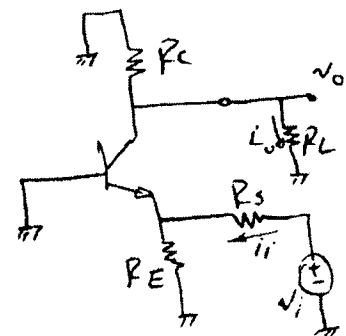
$$r_e = \frac{\alpha}{g_m} \approx \frac{1}{g_m} = \frac{1}{33.52\text{ mA/V}} = 29.8\ \Omega$$

If the amplifier is connected in C.B configuration $R_S = R_L = 10\text{ K}\Omega$ the complete circuit is as shown \rightarrow



Ac Analysis

- All capacitor are s-c
 - reduce DC sources
- using T-model



$$R_i = R_E \parallel R_E = 29.8 \parallel 10K \approx 29.7 \approx R_E$$

$$R_o|_{V_i=0} = R_C = 10K\Omega$$

$$\text{To find } A_v = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{be} (R_C \parallel R_L)$$

$$V_{be} = -V_i \left(\frac{R_E \parallel R_E}{R_E \parallel R_E + R_s} \right) = \frac{-V_i R_i}{R_i + R_s}$$

$$V_o = +g_m V_i \frac{R_i}{R_i + R_s} (R_C \parallel R_L)$$

$$A_v = \frac{V_o}{V_i} = g_m \frac{R_i}{R_i + R_s} (R_C \parallel R_L)$$

$$= 33.52 \times 10^3 \frac{29.7}{29.7 + 10K} (10K \parallel 10K) \approx 0.5 \text{ V/V}$$

$$\text{To find } A_i = \frac{I_o}{I_i}$$

$$I_o = -g_m V_{be} \left(\frac{R_C}{R_C + R_L} \right)$$

$$V_{be} = -I_i R_i$$

$$I_o = +g_m I_i R_i \left(\frac{R_C}{R_C + R_L} \right)$$

$$A_i = \frac{I_o}{I_i} = g_m R_i \frac{R_C}{R_C + R_L}$$

$$= 33.52 \times 10^3 \times 29.7 \frac{10K}{10K + 10K}$$

$$= 0.5 \text{ A/A}$$